# Application of Electron Spin Resonance Spectroscopy to Problems of Structure and Conformation. XV. Conformational Analysis of Semidiones Derived from Cyclobutane, Cyclopentane, Cyclohexane, and Cycloheptane ${ }^{1,2}$ 

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#### Abstract

The effect of temperature on the esr spectra of a number of medium-sized cycloalkanesemidiones has been investigated. The effect of temperature on the population of the equatorial (more stable) and axial conformations of the methylcyclohexanesemidiones yields enthalpy differences of 0.7 and $1.4 \mathrm{kcal} / \mathrm{mole}(\Delta S \cong 0$ ) for the 3- and 4-methyl substituents. The treatment is extended to di- and trialkylated cyclohexanesemidiones. Cyclohexanesemidione and several symmetrically substituted derivatives yielded coalescence temperatures and demonstrated line-broadening effects above and below the coalescence temperature. Coalescence temperatures occur at conformational lifetimes of $\sim 10^{-7} \mathrm{sec}$. Cyclohexanesemidione undergoes the interconversion of halfchair conformations with an enthalpy of activation of $4.0 \mathrm{kcal} / \mathrm{mole}$, entropy of activation $+1 \mathrm{eu} . \quad 3,3$-Dimethyl- or 4,4-dimethylcyclohexanesemidiones have similar enthalpies of activation ( $3.9,3.2 \mathrm{kcal} / \mathrm{mole}$ ) but less favorable entropies of activation ( $-6,-8 \mathrm{eu}$ ). 3,3,5,5-Tetramethylcyclohexanesemidione has an enthalpy of activation of only $2.6 \mathrm{kcal} /$ mole but the entropy of activation for ring inversion is -8 eu . The treatment has been extended to N -methylpiperidine- 3,4 -semidione which is much more conformationally stable than cyclohexanesemidione (coalescence temperature $\sim+60$ and $-85^{\circ}$, respectively) and to cycloheptanesemidione for which a coalescence temperature could not be observed because of conformational stability.


The oxidation of a variety of ketones in basic solution involves paramagnetic intermediates that have been shown by electron spin resonance spectroscopy to be semidiones (1). ${ }^{3}$ The semidiones can also be con-

veniently prepared by the reaction of strong bases with many $\alpha$-diketones and/or $\alpha$-hydroxy ketones in the absence of oxygen. By analysis of the esr spectra, it has been possible to gain a considerable amount of information regarding the structure and conformation of many acyclic and cyclic semidiones, including those derived from steroidal ketones. ${ }^{4-6}$ We have now studied the effect of temperature on the esr spectra of several cyclic semidiones with medium-sized rings in order to obtain thermodynamic data from the rate and equilibrium constants for the ring inversion process. The effect of temperature on the esr spectra of systems capable of undergoing conformational change reveals two distinct behavior patterns depending on whether the possible conformations are equally or unequally populated. For unsymmetrical radicals, e.g., 4-methylcyclohexanesemidione (2), wherein two conformations (e and a) of unequal energy exist in rapid equilibrium, the observed hyperfine splitting constant (hfsc) for a particular proton $\left(a_{o b s d}{ }^{H *}\right)$ is the time average of two
(1) Aliphatic Semidiones. VII.
(2) This work was supported by grants from the National Science Foundation (G12308, GP1579, GP6402X), the National Institutes of Health (GM-13000), and the Petroleum Research Fund (1760-C).
(3) G. A. Russell, E. T. Strom, E. R. Talaty, K.-Y. Chang, R. D. Stephens, and M. C. Young, Record Chem. Progr., (Kresge-Hooker Sci. Lib.), 27, 3 (1966)
(4) E. R. Talaty and G. A. Russell, J. Am. Chem. Soc., 87, 4867 (1965).
(5) E. R. Talaty and G. A. Russell, J. Org. Chem., 31, 3455 (1966).
(6) G. A. Russell, E. R. Talaty, and R. Horrocks, ibid., 32, 353 (1967).
limiting values $a_{\mathrm{e}}{ }^{\mathrm{H} *}$ and $a_{\mathrm{a}}{ }^{\mathrm{H} *}$. The probability ( $f$ ) of the radical existing in conformation e can be easily calculated provided the limiting values of the hfsc are

known (eq 1). A change in temperature usually results

$$
\begin{equation*}
f=\left(a_{\text {obsd }}{ }^{\mathrm{H} *}-a_{\mathrm{a}}{ }^{\mathrm{H}^{*}}\right) /\left(a_{\mathrm{e}}{ }^{\mathrm{H}^{*}}-a_{\mathrm{a}}^{\mathrm{H}^{*}}\right) \tag{l}
\end{equation*}
$$

in a change in the position of the ring inversion equilibrium ( $K_{\mathrm{a}}$ ) with a resulting change in $a_{\text {obsd }}{ }^{{ }^{*}}$. If, however, the two conformations are of equal energy and hence equally populated, as in the case of 3,3 dimethylcyclohexanesemidione (3), then the mean lifetime of a particular conformation ( $\tau_{\mathbf{A}}$ or $\tau_{\mathbf{B}}$ ) is

the reciprocal of the rate constant $\left(k_{\mathbf{A}}\right.$ or $\left.k_{\mathbf{B}}\right)$. If rates are sufficiently rapid (i.e., lifetimes sufficiently short) line-width alternation will occur, ${ }^{7}$ and under these conditions the increase in full line width at half-height $\left(\Delta \omega_{1 / 2}\right)$ of the central absorption peak relative to the wing peaks is related to the mean lifetimes of each conformation by eq 2

$$
\begin{equation*}
\left(\tau_{\mathbf{A}}+\tau_{\mathbf{A}}\right) / \tau_{\mathbf{B}} \tau=\pi(\Delta \nu)^{2} / \Delta \omega_{1 / 2} \tag{2}
\end{equation*}
$$

(7) (a) A Carrington, Mol. Phys., 5, 425 (1962); (b) G. K. Fraenkel, J. Phys. Chem., 71, 139 (1967); (c) J. A. Pople, W. G. Schneider, and H. J. Bernstein, "High Resolution Nuclear Magnetic Resonance," McGraw-Hill Book Co., Inc., New York, N. Y., 1959, Chapter 10; (d) A. Allerhand, H. S. Gutowsky, J. Jonas, and R. A. Meinzer, J. Am. Chem. Soc., 88, 3185 (1966).
where $\Delta \nu$ is the difference (cycles per second) between the limiting values of the axial and equatorial hfsc. ${ }^{7 \mathrm{~d}}$ Converting cycles per second to gauss, substituting $k=k_{\mathbf{A}}=k_{\mathbf{B}}$, and rearranging yields eq 3 wherein $\gamma$ is the gyromagnetic ratio of the electron ( $17.6 \times 10^{6}$ radians $/ \mathrm{gauss} / \mathrm{sec}$ ). When the width is mea-

$$
\begin{equation*}
k=\gamma\left(a_{\mathbf{A}}{ }^{\mathrm{H}}-a_{\mathbf{B}}^{\mathrm{H}}\right)^{2} / 4 \Delta \omega_{1 / 2} \tag{3}
\end{equation*}
$$

sured in gauss between the maximum and minimum of the first derivative spectrum, $k$ ( $\mathrm{sec}^{-1}$ ) is given by eq 4

$$
\begin{equation*}
k=2.54 \times 10^{6}\left(a_{\mathbf{A}}{ }^{\mathrm{H}}-a_{\mathbf{B}}{ }^{\mathrm{H}}\right)^{2} / \Delta \text { width } \tag{4}
\end{equation*}
$$

if the line shape is Lorentzian.
As the exchange rate decreases and the lifetime of a conformational state becomes comparable with the reciprocal of the difference in coupling constants, the expression for the fast exchange line broadening becomes less precise and at the coalescence temperature (the temperature at which the originally degenerate line first separates into a doublet) the rate constant ( $\mathrm{sec}^{-1}$ ) is given by expression $5 .^{7 \mathrm{c}}$ Below the coales-

$$
k=\gamma\left(a_{\mathbf{A}}{ }^{\mathrm{H}}-a_{\mathbf{B}}{ }^{\mathrm{H}}\right) / 2^{2 / 2}=6.22 \times 10^{\mathrm{f}}\left(a_{\mathbf{A}}{ }^{\mathrm{H}}-a_{\mathbf{B}}^{\mathrm{H}}\right)
$$

cence temperature, separate coupling constants can be observed for hydrogen atoms that spend most of their time in axial $\left(a_{\mathrm{a}}{ }^{\mathrm{H}}\right)$ or equatorial $\left(a_{\mathrm{e}}{ }^{\mathrm{H}}\right)$ positions. The rate constant under this condition of slow exchange is given by eq $6 .^{7 c}$

$$
\begin{equation*}
k=6.22 \times 10^{6}\left[\left(a_{\mathbf{A}}{ }^{\mathrm{H}}-a_{\mathbf{B}}{ }^{\mathrm{H}}\right)^{2}-\left(a_{\mathrm{a}} \mathrm{H}-a_{\mathrm{e}}^{\mathrm{H}}\right)^{2}\right]^{1 / 2} \tag{6}
\end{equation*}
$$

## Results

Cyclobutane and Cyclopentanesemidiones. These semidiones are readily prepared by the treatment of the $\alpha$-hydroxy ketones or $\beta$-acetoxy ketones with potassium $t$-butoxide in DMSO or DMF. ${ }^{6,8}$ As expected, both spectra consisted of a quintet of sharp lines having intensity ratios of $1: 4: 6: 4: 1$. This intensity ratio remained unchanged between +70 and $-90^{\circ}$. If any conformational changes are involved, they must involve an inversion frequency much greater than the difference between the extreme values of the coupling constants for a given hydrogen atom in the two conformations. For cyclobutanesemidione no significant temperature effect on the value of the hfsc is observed, while for cyclopentanesemidione a gradual increase in the hfsc is noted as the temperature is lowered (Table I).

Table 1. Variation of Coupling Constant with Temperature ${ }^{a}$

| $\text { Temp, }{ }^{\circ} \text { Cyc }$ | $a^{\mathrm{H}}$, gauss | $\begin{aligned} & \text { _Cyclope } \\ & \text { Temp, }{ }^{\circ} \mathrm{C} \end{aligned}$ | $\begin{gathered} \text { nesemidione-- } \\ a^{\mathrm{H}} \text {, gauss } \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| +70 | $13.52 \pm 0.04$ | +85 | $12.92 \pm 0.04$ |
| +50 | $13.57 \pm 0.03$ | +60 | $12.92 \pm 0.04$ |
| +30 | $13.55 \pm 0.04$ | +35 | $12.95 \pm 0.03$ |
| +10 | $13.60 \pm 0.04$ | +10 | $12.97 \pm 0.06$ |
| -30 | $13.60 \pm 0.03$ | $-15$ | $13.00 \pm 0.03$ |
| -50 | $13.61 \pm 0.04$ | -40 | $13.08 \pm 0.04$ |
| -70 | $13.60 \pm 0.03$ | -65 | $13.15 \pm 0.06$ |
| -90 | $13.67 \pm 0.14$ | -90 | $13.20 \pm 0.07$ |

[^0](8) G. A. Russell, R. D. Stephens, and E. R. Talaty, Tetrahedron Letters, 1139 (1965).

Cyclohexanesemidiones with Unequally Populated Conformations. The esr spectrum of $4-t$-butylcyclohexanesemidione at $25^{\circ}$ in DMSO solution has been reported previously. ${ }^{4,9}$ In DMF solution at $25^{\circ}$, the intensity ratio of the seven lines is $1: 2: 2.9: 4.1: 2.9$ : 1.9:0.9, in good agreement with the spectrum expected for two pairs of hydrogen atoms with one pair ( $a_{\mathrm{a}}{ }^{\mathrm{H}}$ ) having twice the hfsc of the other pair ( $a_{\mathrm{e}}^{\mathrm{H}}$ ). A similar spectrum is observed for the $\Delta^{2,3}$-semidione in the decalin system and in the $\Delta^{2,3}$-semidiones in the 19 -nor steroids. ${ }^{4}$ The fortuitous ratio of $a_{\mathrm{a}}{ }^{\mathrm{H}} / a_{\mathrm{e}}{ }^{\mathrm{H}}=2.0$ in the half-chair conformation of cyclohexanesemidione reflects the dihedral angles for axial and equatorial hydrogens ( $\theta_{\mathrm{a}}, \theta_{\mathrm{e}}$ ) since the hfsc are given by eq $7 .{ }^{9-11}$

$$
\begin{equation*}
a^{\mathrm{H}}=\rho_{\mathrm{C}} B\left\langle\cos ^{2} \theta\right\rangle \tag{7}
\end{equation*}
$$

It follows that $a_{\mathrm{a}}{ }^{\mathrm{H}} / a_{\mathrm{e}}{ }^{\mathrm{H}}=\left\langle\cos ^{2} \theta_{\mathrm{a}}\right\rangle /\left\langle\cos ^{2} \theta_{\mathrm{e}}\right\rangle$. If it is assumed that torsional vibrations within the conformation are small (i.e., $\left\langle\cos ^{2} \theta\right\rangle=\cos ^{2} \theta$ ) then the equilibrium dihedral angle for an axial hydrogen atom is $14^{\circ} .9$ The intensity ratio observed for $4-t$-butylcyclohexanesemidione is practically invariant with temperature. However, the total width of the spectrum showed a consistent change with temperature (see Table II). The constancy of the intensity ratio (i.e., the ratio $a_{\mathrm{a}}{ }^{\mathrm{H}}\left(a_{\mathrm{e}}{ }^{\mathrm{H}}\right)$ is taken as evidence of the population of only one conformation for $4-t$-butylcyclohexanesemidione over the temperature range studied (with the $4-t$-butyl group in the equatorial position) and for the absence of significant torsional motion in this conformation. ${ }^{12}$ It has been assumed that at all temperatures, unstrained cyclohexanesemidiones will possess hfsc for purely axial and equatorial $\alpha$-hydrogen atoms with a ratio of 2.0.

Table II, Variation of Total Spectrum Width of 4-t-Butylcyclohexanesemidione with Temperature ${ }^{a}$

| Temp, ${ }^{\circ} \mathrm{C}$ | $2 a_{\mathrm{a}}{ }^{\mathrm{H}}+2 a_{\mathrm{e}}{ }^{\mathrm{H}}$, gauss | $a_{\mathrm{a}}{ }^{\mathrm{H}}$ (calcd) ${ }^{b}$ |
| :---: | :---: | :---: |
| +90 | $39.4 \pm 0.1$ | $13.13 \pm 0.03$ |
| +70 | $39.6 \pm 0.1$ | $13.20 \pm 0.03$ |
| +50 | $39.7 \pm 0.1$ | $13.23 \pm 0.03$ |
| +10 | $39.7 \pm 0.1$ | $13.23 \pm 0.03$ |
| -30 | $40.0 \pm 0.1$ | $13.33 \pm 0.03$ |
| -60 | $40.25 \pm 0.1$ | $13.41 \pm 0.03$ |

${ }^{a}$ In dimethylformamide solution in the presence of potassium $t$-butoxide. ${ }^{b}$ By assuming $a_{\mathrm{a}}{ }^{\mathrm{H}}=2 a_{\mathrm{e}}{ }^{\mathrm{H}}$.

The esr spectra of 3- and 4-methylcyclohexanesemidiones show a significant effect of temperature. This appears reasonable because in both instances an unequally populated mixture of conformations is expected ( $\mathbf{2} \mathrm{e} \rightleftarrows \mathbf{2 a}, 4 \mathrm{e} \rightleftarrows 4 \mathrm{a}$ ). ${ }^{4} \quad$ Figure 1 gives the esr spectra


[^1]

Figure 1. First derivative esr spectra of 3-methylcyclohexanesemidione (top) and 4 -methylcyclohexanesemidione (bottom) observed in dimethyl sulfoxide solution at $25^{\circ}$ in the presence of 0.1 M potassium $t$-butoxide.


Figure 2. Computer least-squares plot of $\log K_{\mathrm{a}}$ (Table III) $v s$. $1 / T$ for 3 - and 4-methylcyclohexanesemidiones.
observed for these semidiones at $25^{\circ}$. Upon cooling, the spectrum for 4 -methylcyclohexanesemidione approaches that of $4-t$-butylcyclohexanesemidione (i.e., 7 lines, $1: 2: 3: 4: 3: 2: 1$ ). The conformation population fraction ( $f$ ) has been calculated (Table III) by assuming that at all temperatures $a_{\mathrm{a}}{ }^{\mathrm{H}}=2 a_{\mathrm{e}}{ }^{\mathrm{H}}$. For

Table III. Effect of Temperature on Hyperfine Splitting Constants of 3- and 4-Methylcyclohexanesemidiones in Dimethylformamide Solution

| Sub- <br> stituent | Obsd hfsc <br> Triplet <br> Doublet |  |  |  |  | $f_{\mathrm{e}}$ |
| :--- | ---: | ---: | ---: | :--- | :--- | :--- |

[^2]

Figure 3. First derivative esr spectrum observed at $25^{\circ}$ from oxidation of cis- or trans-3,5-dimethylcyclohexanone in dimethyl sulfoxide solution containing potassium $t$-butoxide. Hyperfine splitting constants are given in gauss.

4-methylcyclohexanesemidione the total spectrum width ( $\left.\Sigma a^{H}\right)$ is $2\left(a_{\mathrm{a}}{ }^{\mathrm{H}}+a_{\mathrm{e}}{ }^{\mathrm{H}}\right)$. It thus follows that $a_{\mathrm{a}}{ }^{\mathrm{H}}$ $=\Sigma a^{\mathrm{H}} / 3$. For 3-methylcyclohexanesemidione the sum of the two observed hfsc should be equal to $1.5 a_{\mathrm{a}}{ }^{\mathrm{H}}$. Using the values of $a_{\mathrm{a}}{ }^{\mathrm{H}}$ and $a_{\mathrm{e}}{ }^{\mathrm{H}}$ obtained in this manner in eq 1 yielded the values of $K_{\mathrm{a}}$ given in Table III. The values of $K_{\mathrm{a}}$ summarized in Table III have been plotted in Figure 2 and yield enthalpy differences of $H_{\mathrm{a}}-H_{\mathrm{e}}=1.4 \mathrm{kcal} / \mathrm{mole}$ for 2 and $H_{\mathrm{a}}-H_{\mathrm{e}}=$ $0.7 \mathrm{kcal} /$ mole for 4 . In both cases $S_{\mathrm{a}}-S_{\mathrm{e}}=0.5$ $\pm 0.5 \mathrm{eu}$. The lower conformational stability of the 3-methyl isomer relative to the 4 -methyl isomer is presumably due to the methyl-oxygen eclipsing that occurs in 4 e and which destabilizes 4 e relative to 2 e by about $0.7 \mathrm{kcal} /$ mole. ${ }^{4}$

3,5-Dimethylcyclohexanesemidione is a more complicated system since epimerization of the cis and trans isomers can occur. Treatment of a mixture of isomers of 2-hydroxy-3,5-dimethylcyclohexanone with potassium $t$-butoxide in DMF solution yields the spectrum shown in Figure 3. An elementary consideration of the conformational stabilities of the cis- and transsemidiones (5ee very much more stable than 5aa, 6ae somewhat more stable than 6ea) leads to the structural assignment of Figure 3. Conformation 5ee should possess two large ( $a_{\mathrm{a}}{ }^{\mathrm{H}}$ ) and one small ( $a_{\mathrm{e}}{ }^{\mathrm{H}}$ ) hfsc while 6ae should possess two small $\left(a_{\mathrm{e}}{ }^{\mathrm{H}}\right)$ and one large $\left(a_{\mathrm{a}}{ }^{\mathrm{H}}\right)$ hfsc. As would be expected the spectrum assigned to 5 showed little change of hfsc with temperature indicating that $H_{5 a a}-H_{5 e e}$ must be $>2.5$ $\mathrm{kcal} / \mathrm{mole}$. However, the spectrum assigned to 6 changed with temperature as expected for an equilibrium between 6ae and 6ea. Treatment of the hfsc assigned to 6 in the manner previously employed for the monomethylcyclohexanesemidiones yielded $H_{\mathrm{ea}}-H_{\mathrm{ae}}$ $=1.4 \pm 0.2 \mathrm{kcal} / \mathrm{mole}$ and $S_{\mathrm{ae}}-S_{\mathrm{ea}}=-1.0 \pm 0.5 \mathrm{eu}$.

The use of 3 - and 4 -methylcyclohexanesemidiones as models for the conformational preference of the methyl groups in trans-3,5-dimethylcyclohexanesemidione leads to a prediction of $\Delta H^{\circ}=0.7 \pm 0.4 \mathrm{kcal} /$ mole ( $1.4 \pm 0.2-0.7 \pm 0.2$ ). In a similar fashion it would be predicted that $H_{5 a \mathrm{a}}-H_{5 e \mathrm{e}}=2.1 \pm 0.4$ $\mathrm{kcal} / \mathrm{mole}$ (plus whatever destabilization results from
the 1,3-diaxial interaction of methyl groups in 5aa). Temperature has an effect on the ratio of the two semidiones depicted in Figure 3. This is undoubtedly due to the epimerization equilibrium defined as $K_{\text {ep }}=$ cis-semidione (5)/trans-semidione (6). Figure 4 demonstrates the effect of temperature on this cis/trans ratio and that $H_{6}-H_{5}=0.85 \pm 0.2 \mathrm{kcal} / \mathrm{mole}, S_{6}-S_{5}$ $=1 \pm 0.5 \mathrm{eu}$. Since 6 exists mainly in the 6ae conformation, an enthalpy difference of about $0.85 \mathrm{kcal} /$ mole has been assigned to $H_{5 \text { ee }}-H_{6 a e}$. We thus have the approximate experimental enthalpy differences given in kilocalories per mole.


The conversion of 6ea into 5 aa will involve the conversion of the 3-methyl group from an equatorial to an axial position ( $\Delta H^{\circ}=+0.7$ to $+0.9 \mathrm{kcal} /$ mole $)$ and the introduction of a 1,3-diaxial interaction of two methyl groups which we will presently show requires at least $1 \mathrm{kcal} / \mathrm{mole}$ in the cyclohexene ring. Thus the conversion of 6ea into 5aa should be endothermic by at least $1.8 \mathrm{kcal} / \mathrm{mole}$ and the conversion of 5ee into 5 aa endothermic by at least $0.85+1.4+1.8 \cong 4 \mathrm{kcal} /$ mole.

3,5,5-Trimethylcyclohexanesemidione (7e) and 3,3,5trimethylcyclohexanesemidione (8e) appear to have


$$
a^{\mathrm{H}}=13.1,11.3,5.6 \text { gauss }
$$



Be
$a^{\mathrm{H}}=12.2,5.8$ gauss
single populated conformations at $25^{\circ}$. Semidione 7 was prepared from the acyloin and examined from 90 to $-90^{\circ}$. Over this temperature range the ratios of the three doublet splittings did not change. We conclude that the other possible conformation, 7 a , is at least $2.5 \mathrm{kcal} /$ mole less stable than 7 e . Oxidation of


7 a


8a

3,5,5-trimethylcyclohexanone in DMSO solution containing potassium $t$-butoxide yielded a mixture of 7 e and 8 e . Again the ratio of the two hfsc assigned to $\mathbf{8 e}$ did not change with temperature and it is concluded that 8 a is at least $2.5 \mathrm{kcal} / \mathrm{mole}$ less stable than 8 e .

Oxidation of 2-methyl-5-isopropylcyclohexanone in DMSO solution produces a mixture of two radical anions assigned the trans (9) and cis (10) structures. If the hfsc for a pure axial hydrogen is taken as 13.10 gauss at $25^{\circ}$ in DMSO, ${ }^{4}$ the ratio 9ee/9ae is calculated to be 8.4. The sum of $a_{\mathrm{a}}{ }^{\mathrm{H}}+a_{\mathrm{e}}{ }^{\mathrm{H}}$ for $\mathbf{1 0}$ of $\mathbf{1 7 . 5}$ gauss indicates a geometry of 10ae and/or 10ea which has deviated considerably from the geometry of the unstrained semidiones $\left(a_{\mathrm{a}}{ }^{\mathrm{H}}+a_{\mathrm{e}}{ }^{\mathrm{H}}=19.65\right.$ gauss in DMSO, $25^{\circ}$ ). However, if it is assumed that $a_{a}{ }^{H}$


Figure 4. Computer plot of $\log K_{\mathrm{ep}}=\log ([5 / /[6])$ for cis- and trans-3,5-dimethylcyclohexanesemidiones.
$=2 a_{\mathrm{e}}{ }^{\mathrm{H}}$ for $\mathbf{1 0}$ then a pure axial hydrogen will have a hfsc of 11.6 gauss and the ratio $10 \mathrm{ea} / \mathbf{1 0 a e}$ is calculated to be 5.8. The free-energy differences at $25^{\circ}$ suggest that 9ee is more stable than 9aa by $1.3 \mathrm{kcal} / \mathrm{mole}$ and

that $10 e \mathrm{a}$ is more stable than 10 ae by $1 \mathrm{kcal} / \mathrm{mole}$. Using these data alone leads to the conclusion that an equatorial 3-methyl group is preferred over an axial 3methyl group by $0.15 \mathrm{kcal} / \mathrm{mole}$ and the equatorial 3 -isopropyl group preferred over the axial 3-isopropyl group by $1.15 \mathrm{kcal} / \mathrm{mole}$.

Symmetrically Substituted Cyclohexanesemidiones. The esr spectra of cyclohexanesemidione, 3,3-dimethylcyclohexanesemidione, 4,4-dimethylcyclohexanesemidione, and 3,3,5,5-tetramethylcyclohexanesemidione have been investigated at various temperatures. One problem encountered in the low-temperature studies of both symmetrical and unsymmetrical semidiones was the adverse effect of low temperature on the concentration of the semidione. The effect of temperature on the concentration of radical anion was completely reversible below $25^{\circ}$ and is apparently connected with the equilibrium


The disproportionation reaction of the radical anion must be strongly exothermic. Measurement of the equilibrium constant for the semidione disproportionation probably is complicated by the occurrence of other oxidation-reduction processes, such as the following.


Reactions of this type are apparently involved in the spontaneous formation of semidiones from $\alpha$-hydroxy ketones in basic solution.

As was previously demonstrated for the cyclohexyl radical, ${ }^{13}$ when hydrogen atoms exchange nonidentical environments at a frequency comparable to the difference in their hfsc, line broadening is observed. Figure 5 illustrates the phenomenon for 3,3-dimethylcyclohexanesemidione wherein the interconversion of 3A and $3 B$ causes axial and equatorial hydrogen atoms to exchange places. At $70^{\circ}$ the interconversion of 3A


Figure 5. First derivative esr spectrum of 3,3-dimethylcyclohexanesemidione formed by disproportionation of 2-hydroxy-6,6-dimethylcyclohexanone in dimethylformamide solutions of cesium $t$-butoxide.
and 3B is fast and the $\alpha$ hydrogens are magnetically equivalent ( $a^{\mathrm{H}}=9.3$ gauss) and on a time-average basis spend equal times in axial and equatorial positions. Upon cooling, the central peak broadens until at $-42^{\circ}$ a coalescence temperature is reached. Below the coalescence temperature the central peak splits into a doublet which becomes sharper as the temperature is decreased until four lines of equal intensity with $a_{\mathrm{a}}{ }^{\mathrm{H}}$ $=13.00$ and $a_{\mathrm{e}}{ }^{\mathrm{H}}=6.50$ are observed. In a similar manner 4,4-dimethylcyclohexanesemidione yielded a coalescence temperature of $-62^{\circ}$ and at high temperature a quintet splitting of 9.46 gauss. 3,3,5,5Tetramethylcyclohexanesemidione gave a triplet splitting of 8.88 gauss at $+90^{\circ}$ and a coalescence temperature of $-85^{\circ}$. Figure 6 illustrates the effect of temperature on cyclohexanesemidione which shows a $1: 4: 6: 4: 1$ quintet at $25^{\circ}, a^{\mathrm{H}}=9.65$ gauss in DMF. The second and fourth peaks broaden as the temperature is lowered until at $-85^{\circ}$ an approximately $1: 4: 1$ trip-
(13) R. W. Fessenden and R. H. Schuler, J. Chem. Phys., 39, 2147 (1963).


Figure 6. First derivative esr spectra of cyclohexanesemidione prepared by disproportionation of 2-hydroxycyclohexanone in dimethylformamide solutions of cesium $t$-butoxide. Note the decrease in signal intensity as reflected by the signal-to-noise ratio upon cooling.
let is observed for the six magnetic transitions that are unaffected when axial and equatorial hydrogens are interchanged. Below this temperature a seven-line spectrum was observed which approached the $1: 2: 3: 4$ : $3: 2: 1$ multiplicity observed for the frozen conformation of 4-t-butylcyclohexanesemidione at $25^{\circ}$.

Treatment of the line-broadening data above the coalescence temperature (eq 4 ), the coalescence temperature (eq 5), and peak separation below the coalescence temperature (eq 6) yielded rate constants for the ring inversion process plotted in Figure 7. Thermodynamic data obtained from Figure 7 is summarized in Table IV. The significantly lower value of $\Delta H^{\neq}$

Table IV. Activation Parameters for Ring Inversion of Symmetrically Substituted Cyclohexanesemidiones

|  |  |  |  | $\Delta F \neq$ at <br> coales- <br> cence |
| :--- | :---: | :---: | :---: | :---: |
| Substituent | $\Delta H \neq$, <br> $\mathrm{kcal} /$ <br> mole | Coales- <br> cence <br> temp, <br> kcal/ <br> momp, |  |  |
| None | 4.0 | +1.0 | -85 | 3.8 |
| 3,3-Dimethyl | 3.9 | -6.0 | -62 | 2.6 |
| 4,4-Dimethyl | 3.2 | -8.0 | -42 | 1.4 |
| 3,3,5,5-Tetra- | 2.6 | -8.0 | -85 | 1.2 |
| methyl |  |  |  |  |

for the 3,3,5,5-tetramethylcyclohexanesemidione appears to be connected with the diaxial interactions of the methyl groups. It appears this interaction may destabilize 11 by as much as $2.5 \mathrm{kcal} /$ mole (see previous

section). This interaction may also change (i.e., flatten) the geometry of the cyclohexene half-chair structure. This is apparent from the fact that $a_{\mathrm{a}}{ }^{\mathrm{H}}$ $+a_{e}{ }^{H}$ for 11 was 17.74 gauss at $90^{\circ}$, whereas for the other three cyclohexanesemidiones studied this sum was $19.1 \pm 0.2$ gauss. Unfortunately the 3,3,5,5-tetra-


Figure 7. Computer least-squares plot of $\log k / T$ vs. $1 / T$ for the conformational interconversion of symmetrically substituted cyclohexanesemidiones.
methylcyclohexanesemidione could not be studied at a low enough temperature to ascertain if the ratio $a_{\mathrm{a}}{ }^{\mathrm{H}} /$ $a_{\mathrm{e}}{ }^{\mathrm{H}}$ deviated substantially from 2.0 , as the other data suggest to be the case.

If the 1,3 -diaxial interaction of the methyl groups in 11 destabilizes this semidione by $2.5 \mathrm{kcal} / \mathrm{mole}$ relative to the cyclohexanesemidione, it follows from the activation parameters of Table IV that such destabilization is reduced in the transition state to $1.1 \mathrm{kcal} /$ mole ( 2.5 $+2.6=4.0+1.1$ ). It seems reasonable that the transition state would be more planar than 11 and that 1,3-diaxial interactions as well as alkyl-oxygen eclipsings will be reduced in the transition state.

The rates of ring inversion of 3,3,5,5-tetramethylcyclohexanesemidione were studied in dimethyl sulfoxide, DMF, and 1,2-dimethoxyethane solutions from 0 to $80^{\circ}$ with the gegenions cesium, rubidium, and potassium. In this temperature range solvent or gegenions had little if any effect on the rate constant. With lithium or sodium cations hyperfine splitting due to the gegenion was detected at $25^{\circ}$. In DMSO at $80^{\circ}$ the splitting by these cations was not observed and rate constants were measured that were within experimental uncertainty equivalent to the rate constants measured with the other cations.
$\mathbf{N}$-Methylpiperidine-3,4-semidione. The effects of inversion of the nitrogen configuration and of the ring conformation are shown in Figure 8. When the semidione is prepared by oxidation of N -methyl-4-piperidone in DMSO in the presence of base at $25^{\circ}$ only a single semidione is detected with $a^{\mathrm{H}}=6.4,6.6,11.8,13.2$ and $a^{\mathrm{N}} \cong 0.5$ gauss. Upon warming, a coalescence temperature is reached at about $+60^{\circ}$. At $+110^{\circ}$ a $1: 4: 6: 4: 1$ quintet, $a^{\mathrm{H}}=9.25$ gauss, further split by $a^{N}=0.7$ gauss, is observed. It appears certain that above the coalescence temperature the $\alpha$ hydrogen atoms are spending equal time in axial and equatorial positions, e.g., the conformations involved are equally populated. The simplest explanation to


Figure 8. Possible conformational and configurational interconversions for N -methylpiperidine-3,4-semidione.


Figure 9. First derivative esr spectrum of cycloheptanesemidione at $25^{\circ}$ in dimethyl sulfoxide solution. The semidione was prepared by disproportion of 2-hydroxycycloheptanone in the presence of potassium $t$-butoxide. In addition to the two major triplet splittings additional hyperfine splitting, possibly a 0.52 doublet of 0.26 gauss triplets, is observed.
the above facts is that only conformations 12 e and $\mathbf{1 2 e}{ }^{\prime}$ are significantly populated.

It has been shown by nmr spectroscopy that N methylpiperidine exists mainly or completely with the N methyl group in an equatorial position. ${ }^{14}$ Whether the interconversion of 12 e to $12 \mathrm{e}^{\prime}$ involves 12 a or $12 \mathrm{a}^{\prime}$ as an intermediate cannot be answered. However, the greater conformational stability of the N -methylpiperidinesemidione relative to cyclohexanesemidione (coalescence temperature $-85^{\circ}$ ) is apparently due to the requirement of both a ring and a nitrogen atom inversion to convert 12 e into $12 \mathrm{e}^{\prime}$. Whether the nitrogen inversion can occur simultaneously with ring inversion (12e $\rightleftarrows \mathbf{1 2 e}^{\prime}$ ) or must be a slow step following or preceding the ring inversion (12e $\rightarrow \mathbf{1 2 a}^{\prime} \rightarrow \mathbf{1 2 e}^{\prime}$ or $\mathbf{1 2 e} \rightarrow \mathbf{1 2 a} \rightarrow \mathbf{1 2} \mathrm{e}^{\prime}$ ) cannot be specified. It is our feeling that the observed coalescence temperature of $+60^{\circ}$ is connected with the direct process ( $\mathbf{1 2 e} \rightleftarrows \mathbf{1 2} \mathbf{e}^{\prime}$ ) since the conformational lifetimes of $\sim 10^{-7} \mathrm{sec}$ appear too short for a nitrogen inversion process, even the exothermic conversion of $\mathbf{1 2 a}$ into $12 \mathrm{e}^{\prime}$.

Cycloheptanesemidione gave a spectrum (Figure 9) that was a triplet of triplets between +30 and $-80^{\circ}$. As shown in Table V little change in hfsc was observed over the temperature range studied. Cycloheptanesemidione is conformationally more stable than cyclohexanesemidione. This is apparently due to the fact that cycloheptanesemidione can assume a chairlike structure (13) that would be expected to have an energy


[^3]Table V. Hyperfine Splitting Constants for Cycloheptanesemidiones ${ }^{\star}$

| Temp, ${ }^{\circ} \mathrm{C}$ | Hyperfine splitting constants, ${ }^{b}$ gauss <br> Unsubstituted ${ }^{c}$ | 3, 3-Dimethyld |
| :---: | :---: | :---: |
| +60 |  | 10.00 |
| +30 | $6.63,2.00$ | 10.00 |
| +10 | $6.61,2.02$ | 10.00 |
| -20 | $6.62,2.05$ | 10.02 |
| -40 | $6.62,2.05$ | 10.05 |
| -60 | $6.64,2.07$ | 10.05 |
| -80 | $6.61,2.11$ | 10.05 |

${ }^{a}$ Prepared by oxidation of the acyloin in DMF in the presence of potassium $t$-butoxide. ${ }^{b}+0.05$ gauss. ${ }^{c}$ Triplet splittings. ${ }^{d}$ Doublet splitting.
of activation for ring inversion comparable to that of cyclohexane ( $10-12 \mathrm{kcal} / \mathrm{mole}$ ). The dihedral angles for the $\alpha$-hydrogen atoms calculated from the observed hfsc are -51 and $+69^{\circ}$ for the quasi-axial and quasiequatorial carbon-hydrogen bonds (14). ${ }^{15} \mathrm{Nmr}$ spectroscopy has provided a measurement of $\theta_{\mathrm{a}}=-19^{\circ}$ and $\theta_{\mathrm{e}}=79^{\circ}$ for cycloheptene. ${ }^{16}$ For cyclohexene the nmr method yields $\theta_{\mathrm{a}}=-13^{\circ}, \theta_{\mathrm{e}}=47^{\circ},{ }^{16}$ in excellent agreement with the estimates made by esr examination of the semidiones. Since the quasi-axial

hydrogen atoms actually point into the center of the cycloheptene ring, it follows that serious diaxial interactions between the 3,7 positions of the cycloheptene ring may occur. To test this postulate 3,3 -dimethylcycloheptanesemidione was prepared. The spectrum was a doublet of 10.0 gauss between -60 and $+60^{\circ}$. The lines were somewhat broad ( $\sim 2$ gauss) but no further hfs could be detected. We conclude that in 3,3-dimethylcycloheptanesemidione $a_{\mathrm{a}}{ }^{\mathrm{H}}=10.0, a_{\mathrm{e}}{ }^{\mathrm{H}}$ $\ll 1$ gauss. Apparently the methyl at the axial position at $\mathrm{C}-3$ has repelled the axial hydrogen at C-7 until the equatorial hydrogen at $\mathrm{C}-7$ resides close to the nodal plane ( $\theta_{\mathrm{e}}=90^{\circ}$ ). Taking $\theta_{\mathrm{a}}=-30^{\circ}$ for the hydrogen at the 7 position leads to $B \rho_{\mathrm{C}}=12.5$ gauss for 3,3 -dimethylcycloheptanesemidione. The lack of a significant temperature effect on the hfsc as well as a value of $a_{\mathrm{e}}{ }^{\mathrm{H}}$ close to zero rule out significant torsional motion of the $\alpha$-methylene group in cycloheptanesemidione and justify the calculation of dihedral angles via the Heller-McConnell equation.

## Discussion

Cycloheptene apparently has much greater conformational stability than cyclohexene. The results ob-
(15) By simultaneous solution of the Heller-McConnell equations, $a^{\mathrm{H}}=\rho \mathrm{C} B \cos ^{2} \theta$. For cycloheptane there are two possible solutions, $\theta_{\mathrm{a}}=+3^{\circ}, B \rho_{\mathrm{C}}=6.8$ gauss, or $\theta_{\mathrm{a}}=51^{\circ}, B \rho_{\mathrm{C}}=16.4$ gauss. For $4-t^{-}$ butylcyclohexanesemidione only a single solution is realistic; $\theta_{\mathrm{a}}=14^{\circ}$, $B \rho_{\mathrm{C}}=14$ gauss. For cyclopentanesemidione with $\theta_{\mathrm{a}}=30^{\circ}, B \rho \mathrm{c}$ must be 17.6. It seems most reasonable for cycloheptanesemidione that $B \rho_{\mathrm{C}}$ will be 16.4 gauss and that $\theta_{\mathrm{a}}=-51^{\circ}$. We had indicated previously that $\theta_{\mathrm{a}}=+3^{\circ}$ might be the preferred geometry.
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served with cycloalkanesemidiones suggest the possibility of observing 3 or 4 position symmetrically substituted cycloheptenes as optically active disymmetric chromophores.

The temperature effect observed for the hfsc of cyclo-pentane- and cyclohexanesemidiones appears to be connected with some sort of molecular motion since the more rigid cyclobutane- and cycloheptanesemidiones do not show a significant variation in hfsc. However, the interpretation of this effect is by no means obvious. We have argued that it is not the result of torsional or rocking motion of the $\alpha$-methylene group. transBiacetyl radical anion shows a similar temperature effect ( $a_{\mathrm{CH}_{3}}{ }^{\mathrm{H}}$ increases as the temperature is decreased). This excludes a torsional explanation because $a_{\mathrm{CH}_{3}{ }^{H}}$ $=\left(B \rho_{\mathrm{c}} / 3\right)\left[\cos ^{2} \theta+\cos ^{2}\left(\theta+120^{\circ}\right)+\cos ^{2}\left(\theta+240^{\circ}\right)\right]$ is independent of the value of $\theta$. Ion pairing between the semidione and the cation is apparently excluded since trans- and cis-semidiones show similar effects. Population of a transition state conformation (e.g., half-boat conformation for cyclohexane would appear capable of explaining the observed temperature effect for cyclohexanesemidiones but seems incapable of explaining the effect observed for the biacetyl radical anion or cyclopentanesemidione. If the effect of temperature on hfsc is connected with some vibrational motion of the $\alpha$-methylene group, a deviation in $a^{\mathrm{H}} / a^{\mathrm{D}}$ from the value of 6.514 (i.e., the ratio of nuclear magnetic moments) would be expected since the vibrational amplitudes of carbon-hydrogen and carbon-deuterium bonds are different. This should be true whether the vibration is torsional or a breathing vibration involving changes in the $\mathrm{C}_{\pi}-\mathrm{C}_{\alpha}-\mathrm{H}$ angle. Actually, the observed isotope effects are very close to the theoretical value. Preparation of cyclohexanesemidione in DMSO- $d_{6}$ yielded a nonet with intensities 1:4:10:16:19:16: $10: 4: 1$ and $a^{\mathrm{D}}=1.465 \pm 0.005$ gauss at $25^{\circ}$. The value of $a^{\mathrm{H}}$ in DMSO is $9.68 \pm 0.03$ gauss and $a^{\mathrm{H}} / a^{\mathrm{D}}$ $=6.60$.
In a similar fashion cyclopentanesemidione yielded $a^{\mathrm{H}}=13.12 \pm 0.05, a^{\mathrm{D}}=1.00 \pm 0.01, a^{\mathrm{H}} / a^{\mathrm{D}}=6.60$ in DMSO at $25^{\circ}$. We conclude that the value of $a^{\mathrm{H}}$ is not particularly influenced by any vibrational motion of the $\alpha$-carbon-hydrogen bond. Incidentally, the observed hfsc can be interpreted as showing that in situations wherein an unpaired spin is delocalized by hyperconjugation ( $\cdot \mathrm{C}-\mathrm{C}-\mathrm{H}(\mathrm{D}) \leftrightarrow \mathrm{C}=\mathrm{CH} \mathrm{H} \cdot(\mathrm{D} \cdot)$ ) that $\rho_{\mathrm{H}}=\rho_{\mathrm{D}}$, i.e., deuterium and hydrogen undergo hyperconjugation to the same degree.

Perhaps the increase in hfsc with a decrease in temperature is connected with the spin density of the carbonyl carbon atoms. This in turn could be controlled by the planarity of the dicarbonyl system. Both cyclo-butane- and cycloheptanesemidiones have values of $B \rho_{\mathrm{C}}$ greater than cyclohexanesemidione and show little effect of temperature on hfsc. Perhaps these are highly planar structures as far as the four atoms in the $\pi$ system are concerned and $\rho_{\mathrm{C}}$ is a maximum. For cyclohexane, cyclopentane-, and biacetylsemidiones the degree of planarity may increase as the temperature is lowered with a resulting increase in $\rho_{\mathrm{C}}$. If this is the case, it is surprising that the natures of the cation and solvent do not have a larger effect on the value of the hfsc since chelation of a cis-semidione would be expected to increase the planarity of the system.

We have assumed from elementary considerations of nonbonding interactions that the preferred conformation of cycloheptanesemidione is that resembling a chair structure. ${ }^{17}$ However, our results do not exclude the conformation 15. ${ }^{18}$ Boat conformations of cyclo-


15
heptene derivatives are required to explain certain solvolytic results, for example, the conversion of 4cycloheptenylmethyl derivatives to endo-2-bicyclo[3.2.1]octane derivatives. ${ }^{19}$ However, there is no evidence of participation by the double bond in the products observed from 4 -cycloheptenyl brosylate. ${ }^{20}$

Extensive long-range hfs has been noted in bicyclic and tricyclic semidiones that could be taken as models for $\mathbf{1 3}$ and 15. ${ }^{21,22}$ Bicyclo[3.2.1]octane-6,7-semidione. prepared by oxidation of the monoketone, appears to be a model for 15. In this semidione hfsc of 5.51, 4.03 (two), and 0.53 (three or five) gauss are observed. ${ }^{22}$ The $\beta$ - and $\gamma$-methylene groups are extensively involved.

Tricyclo[3.2.1 ${ }^{3,8}$ ] nonane-6,7-semidione, prepared by oxidation of the monoketone, ${ }^{23}$ gives rise to a complicated spectrum, apparently showing hfs by all ten hydrogen atoms. A possible assignment of hfsc for this model of 13 is $a^{\mathrm{H}}=6.15$ (two), 2.60, 2.34 (two), 0.40 (two), 0.25 (two), and 0.20 gauss. ${ }^{24}$ It thus appears that the observed long-range hfs by $\beta$ - and $\gamma$ hydrogen atoms in cycloheptanesemidione could be consistent with either structure $\mathbf{1 3}$ or $\mathbf{1 5}$.

It is pertinent that a cycloheptene derivative, 1, 1,4,4-tetramethyl-6,7-benzocycloheptene, has been extensively studied by pmr and an enthalpy difference between the chair and boat conformations of only $317 \mathrm{cal} / \mathrm{mole}$ found. ${ }^{25}$ Enthalpies of activation for the interconversion of these conformations (boat $\rightleftarrows$ boat, boat $\rightleftarrows$ chair, chair $\rightleftarrows$ chair) were in the range of $10 \mathrm{kcal} /$ mole, ${ }^{25}$ consistent with our observation of a frozen conformation for cycloheptanesemidione in the time scan of $\sim 10^{-7} \mathrm{sec}$.

A comparison of the enthalpy of activation for ring inversion of cyclohexanesemidione with estimates for cyclohexene ${ }^{26}$ and 4 -bromocyclohexene ${ }^{27}$ is of interest. From pmr spectroscopy a coalescence temperature of $-164^{\circ}$ has been observed for cis-3,3,4,5,6,6- $d_{6}$-cyclohexane in bromotrifluoromethane solution. ${ }^{26}$ This corresponds to a $\Delta H^{\ddagger}$ of $5.3 \mathrm{kcal} /$ mole if $\Delta S^{\ddagger}$ is zero. For 4 -bromocyclohexene a coalescence temperature is observed at $-145^{\circ}$ and a value of $\Delta H^{\ddagger}=6.1 \mathrm{kcal} /$

[^4]mole estimated. ${ }^{27}$ Experimental values of $\Delta H^{\ddagger}$ are $2-3 \mathrm{kcal} / \mathrm{mole}$ lower for the cyclohexanesemidiones. Apparently the lowered double bond character in the semidione (standard HMO calculations indicate a bond order, $1+\Sigma \mathrm{N} c_{i} c_{\mathrm{j}}$, of 1.6 between the carbonyl carbon atoms) facilitates the ring inversion process. The repulsion of the negatively charged oxygen atoms may also contribute to the lowered energy barrier although this effect may be offset by chelation between the semidione and alkali metal cation.

It is difficult to assess the reliability of the values of $\Delta S \neq$ reported in Table IV. The values of $\Delta H \neq$ appear reliable to $\pm 0.5 \mathrm{kcal} / \mathrm{mole}$ and the values of $\Delta F^{\neq}$coales should be accurate to $\pm 0.3 \mathrm{kcal} /$ mole, provided that our approach to the measurement of rate constants from line broadening is valid. It is apparent for cyclohexanesemidione and its 3,3,5,5-tetramethyl derivative that a considerable difference in $\Delta S \neq$ exists (in the range of 9 eu ). In addition to the usual symmetry considerations, variations in the absolute value of $\Delta S^{\mp}$ may reflect ionic association and solvation, as well as restricted motion due to steric considerations in the ground and transition states.

## Experimental Section

Preparation and Detection of Semidiones. Radical anions were prepared by the disproportionation of the appropriate $\alpha$-hydroxy ketones in DMSO containing excess potassium $t$-butoxide or in DMF containing excess cesium $t$-butoxide. ${ }^{4}{ }^{28}$ In a typical experiment equal volumes of deoxygenated solutions of the hydroxy ketone $(0.05 \mathrm{M})$ and base ( 0.1 M ) were mixed in the inverted U-cell described previously. ${ }^{29}$ The esr spectra were measured using a Varian Associates V-4500 epr spectrometer with 100 -kcps field modulation and with a 9 -in. magnet, regulated by a Fieldial control. Variable-temperature experiments were performed using a Varian Associates V-4540 variable-temperature controller which was found to reproducibly yield temperatures within $\pm 1^{\circ}$. The temperature of the sample was calibrated by a copper-constantan thermocouple which was immersed into the sample in the cavity. All spectra were recorded in flat, fused silica cells. At ambient temperatures the Varian Associates V-4548 aqueous sample cell was used. For thermostated experiments a special cell (V-4548-1) to fit within the dewar insert was obtained from Varian Associates.

Field scans were calibrated by $p$-benzosemiquinone in $85 \%$ ethanol ( $a^{\mathrm{H}}=2.368$ gauss). ${ }^{30}$ Line widths were measured as the difference between maxima and minima of the first derivative spectra. The wing peaks of the spectrum were used as internal standards for line width. Other peaks were compared with the standard line widths by alternately scanning the standard and broadened peaks. A large number of scans ( $10-30$ ) were recorded at each temperature. For cyclohexane- and 4,4-dimethylcyclohexanesemidiones the broadened peaks examined were the $M_{\mathrm{I}}= \pm 1$ lines and the standards were the $M_{\mathrm{I}}= \pm 2$ lines. Calculations were based on the average values for the two sets of data. For 3,3 -dimethyl- and 3,3,5,5-tetramethylcyclohexanesemidione the $M_{1}=+1$ and -1 lines were scanned and averaged to yield the standard line width at each temperature. There was a tendency for the standard line width to change with time, perhaps because of exchange broadening. However, $\Delta \omega_{1} / 2$ showed no change with time. We did not find the precision improved by the use of second derivative spectra.

The derivation of eq 4 follows directly from eq $8,{ }^{7 d}$ where $\tau=$ $\tau_{\mathbf{A}} \tau_{\mathbf{B}} /\left(\tau_{\mathbf{A}}+\tau_{\mathbf{B}}\right){ }^{70} P_{\mathbf{A}}$ and $P_{\mathbf{B}}$ are the fractional populations of the two conformations $\mathbf{A}$ and $\mathbf{B}, \delta \nu$ is the difference in hfsc for a given hydrogen atom in conformations $\mathbf{A}$ and $\mathbf{B}$, and $\Delta \omega_{1 / 2}$ is the total line width at half-height for a Lorentzian absorption curve. When

$$
\begin{equation*}
1 / 2 \tau=2 \pi P_{\mathbf{A}} P_{\mathbf{B}}(\delta \nu)^{2}\left(\Delta \omega_{1 / 2}\right)^{-1} \tag{8}
\end{equation*}
$$

$P_{\mathbf{A}}=P_{\mathbf{B}}\left(\tau_{\mathbf{A}}=\tau_{\mathbf{B}}\right)$ it follows that $\tau_{\mathbf{A}}=1 / 2 \tau=k_{\mathbf{A}}$. Substituting $\nu=\gamma H / 2 \pi$ and $\Delta \omega_{1 / 2}=\sqrt{3}(\Delta$ width $)(\gamma / 2 \pi)$ to convert to cycles

[^5]per second and to correct for the difference in full line widths between the absorption curve at half-height and the first derivative curve between maximum and minimum leads to eq 9 which is equivalent to eq 4.
\[

$$
\begin{equation*}
k=\left(17.6 \times 10^{6}\right)\left(a_{\mathbf{A}}{ }^{\mathrm{H}}-a_{\mathbf{B}}^{\mathrm{H}}\right) / 4 \sqrt{3}(\Delta \text { width }) \tag{9}
\end{equation*}
$$

\]

Materials. 2-Acetoxycyclobutanone, ${ }^{81}$ 2-hydroxycyclopentanone, ${ }^{32}$ 2-hydroxy-6-methylcyclohexanone, ${ }^{33}$ 2-acetoxy-4-methylcyclohexanone, ${ }^{34}$ 2-bromo-6,6-dimethylcyclohexanone, ${ }^{35}$ 2-ace-toxy-4,4-dimethylcyclohexanone, ${ }^{36}$ 2-acetoxy-3,5-dimethylcyclohexanone, ${ }^{37}$ 2-hydroxy-3,5,5-trimethylcyclohexanone, ${ }^{38}$ 2-acetoxy-3,3,5,5-tetramethylcyclohexanone, ${ }^{39}$ 2-hydroxycycloheptanone, ${ }^{40}$ 2,2-dimethylcycloheptanone, ${ }^{41}$ and 2 -hydroxymenthone ${ }^{42}$ were prepared according to the literature.
2-Hydroxy-6,6-dimethylcyclohexanone was prepared from the bromo ketone. The bromo ketone ( 100 mg ) was dissolved in ethanol ( 2 ml ) and a solution of potassium carbonate ( 50 mg ) in water ( 1 ml ) was added. The solution was heated to reflux for

[^6]0.5 hr at which time the reaction (monitored by tlc) appeared complete. The solution was cooled and extracted with five 2 -ml portions of methylene chloride. The combined extracts were washed once with water, evaporated free of solvent, and dried by azeotropic distillation with benzene. The crude material was purified by glpc on a 5 -ft column of $20 \% \mathrm{SF}-96$ on firebrick at $180^{\circ}$. The retention time of the product was 11.5 min while under identical conditions the starting material had a retention time of 6.5 min . The product was a colorless liquid: $n^{25}$ D 1.4305 ; mass spectrum, parent peak at m/e 140. Anal. Calcd for $\mathrm{C}_{3} \mathrm{H}_{12} \mathrm{O}_{2}$ : C, 68.6; H, 8.57. Found: $\mathrm{C}, 68.5 ; \mathrm{H}, 8.56$. The ketone gave a phenylhydrazone (methanolwater) of mp 137-139 ${ }^{\circ} \mathrm{dec}$ whose mass spectrum gave a parent peak at m/e 208. Anal. Calcd for $\mathrm{C}_{14} \mathrm{H}_{20} \mathrm{~N}_{2} \mathrm{O}$ : $\mathrm{N}, 13.45$. Found: $\mathrm{N}, 13.5$.

2-Acetoxy-7,7-dimethylcycloheptanone was prepared. 2,2-Dimethylcycloheptanone ( 1 g ) was dissolved in glacial acetic acid ( 300 ml ) and to the mixture was added boron trifluoride diethyl etherate $(6 \mathrm{ml})$ and lead tetraacetate $(1.90 \mathrm{~g})$. The mixture was stirred at room temperature for 4 hr , at $50^{\circ}$ for 4 hr , and at $80^{\circ}$ for 4 hr . The mixture was cooled and the excess of acetic acid was removed at an aspirator. When the volume was reduced to 10 ml , the distillation was stopped, the solution was diluted with water ( 200 ml ) and extracted with four $100-\mathrm{ml}$ portions of benzene. The combined extracts were washed once with saturated sodium bicarbonate solution ( 20 ml ) and once with water ( 10 ml ) and the benzene was removed by distillation. The light brown oil ( 1 g ) was distilled, bp $100^{\circ}(2 \mathrm{~mm})$. Final purification was effected by glpe on a $5-\mathrm{ft}$ column of $20 \%$ SF 96 on firebrick. The retention time of the product was 11.0 min , while that of the starting material under identical conditions was 5.5 min . Anal. Calcd for $\mathrm{C}_{11} \mathrm{H}_{18} \mathrm{O}_{3}$ : $\mathrm{C}, 70.2 ; \mathrm{H}, 9.6$. Found: C, $70.2 ; \mathrm{H}, 9.5$. The ketone yielded a phenylhydrazone, mp 144-145 . Anal. Calcd for $\mathrm{C}_{17} \mathrm{H}_{24} \mathrm{~N}_{2} \mathrm{O}_{2}$ : C, 70.9; H, 8.33. Found, C, 71.2; H, 8.2.

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# Secondary Deuterium Isotope Effects. $\beta$-Kinetic Effects in Sn2 Reactions of $\mathrm{N}, \mathrm{N}$-Dimethylaniline and Dimethylphenylphosphine with Methyl $p$-Toluenesulfonate and Comparison with Observed and Calculated Vibrational Frequencies of Deuterated and Undeuterated Dimethylaniline and Trimethylanilinium Ion ${ }^{1}$ 

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#### Abstract

The rates of reaction, in nitrobenzene at $51.29^{\circ}$, of methyl $p$-toluenesulfonate with $\mathrm{N}, \mathrm{N}$-dimethylaniline end $\mathrm{N}, \mathrm{N}$-dimethyl- $d_{6}$-aniline to form trimethylphenylammonium and methyldimethyl- $d_{6}$-phenylammonium $p$ toluenesulfonates, respectively, and with dimethylphenylphosphine and dimethyl- $d_{6}$-phenylphosphine to form the corresponding phosphonium salts, were determined conductiometrically. The secondary isotope effects observed are small and inverse: $1.133 \pm 0.008$ for the amines, and $1.050 \pm 0.002$ for the phosphines. The result for the amines is discussed in relation to the equilibrium isotope effect calculated using information obtained from the observed infrared spectra of the reactants and products. Though uncertainties in the assignment of spectral bands exist, it appears that there is very little shift in $\mathrm{CH}(\mathrm{CD})$ stretching force constants. The inverse effect is, therefore, very probably due to increased force constants for lower frequency vibrations, such as for bending. This interpretation is consistent with a steric explanation for the isotope effects. Inductive effects are expected to produce changes in the stretching force constants.


TThe origin of secondary deuterium isotope effects ${ }^{3}$ is understood, in terms of the general theory of isotope effects, ${ }^{4}$ to be changes in vibrational force con-
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[^2]:    ${ }^{a} K_{\mathrm{a}}=[2 \mathrm{a}] /[2 \mathrm{e}]$ or [4a]/[4e]. ${ }^{b}$ By use of $a_{\mathrm{a}}{ }^{\mathrm{H}}$ and $a_{\mathrm{e}}{ }^{\mathrm{H}}$ measured for 3,3-dimethylcyclohexanesemidione at $-80^{\circ}$.

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